

Recursion

Asymptotic Time¹ of Operations for Collections of n Elements

	Trivial ArrayList	Good ArrayList	LinkedList
Insert beginning			
Insert end			
Get length			
Get i^{th} element			

1. Funny Greek symbols:
 - a. O : Upper bound: the running time is no *slower* than this. To be useful, make this as small as possible. We can eat breakfast before lecture because breakfast couldn't possibly take more than half an hour.
 - b. Ω : Lower bound: the running time is no *faster* than this. To be useful, make this as large as possible. We can have a party because mom won't be home for at least 3 days.
 - c. Θ : Exact bound. $f = \Theta(g)$ means that $f = O(g)$ and $f = \Omega(g)$.
2. More funny symbols:
 - a. $a * b =$ " a **added** to itself b times"
 - b. $a^b =$ " a **multiplied** by itself b times"
 - c. $a / c =$ "how many times you have to **add** a to itself to produce c "
 - d. $\log_a c =$ "how many times you have to **multiply** a by itself to produce c "
3. Analyze:
 - a. `int f(int x) { if (x <= 0) { return 1; } else { return x * f(x - 1); } }`
 - b. `int g(int x) { if (x <= 0) { return 1; } else { return x * g(x / 2); } }`

¹ Expected, amortized time