

Lisp

CSCI 334
Stephen Freund

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John McCarthy



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IBM 704



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Factorial

- Two cases:
 - base case: n is 0
 - recursive case: $n * \text{fact}(n-1)$
- ```
(defun fact (n)
 (cond ((eq n 0) 1)
 (t (* n (fact (- n 1))))))
```
- ```
(fact 3) -> 6
```

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List Length

- Two cases
 - base case: empty list
 - recursive case: process "car", recurse on "cdr"
- ```
(defun length (l)
 (cond ((eq l nil) 0)
 (t (+ 1 (length (cdr l))))))
```

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## Membership

- Does a list contain a specific atom?
- ```
(contains 'A '(C A M P)) -> t
```
- ```
(contains 'B '(C A M P)) -> nil
```
- ```
(defun contains (x l)
  (cond ((eq x nil) nil)
        ((eq x (car l)) t)
        (t (contains x (cdr l)))))
```

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Lisp (2)

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Recap

- Expressions
 - (+ 1 2 3) → 6
- Lists
 - nil
 - (cons 'A '(B C)) → (A B C)
 - (car '(A B C)) → A
 - (cdr '(A B C)) → (B C)
 - (car (cdr '(A B C))) → B
 - also have length, append, reverse

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Recap (2)

- Conditional
 - (cond (test₁ result₁) ... (test_n result_n))
 - tests:
 - (eq x y)
 - (< x y)
 - (atom x) (will want to use in problem set)
- Functions
 - (defun cube (x) (* x x x))
 - [sheep]
- (division)
- (wrap up insertion-sort)

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Notes

- Book uses slightly different dialect of Lisp
- Use class notes as a reference, or the Lisp tutorial on the web site.
- Major differences
 - use T instead of true
 - use (defun ...) instead of (define ...)
 - use (mapcar #'f l) instead of (maplist f l)

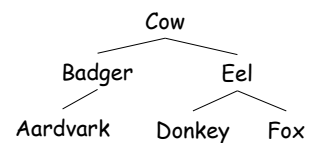
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Insert

- Insert a number into a sorted list
- (insert 4 '(1 3 7)) → (1 3 4 7)
- (defun insert (x l)
 (cond ((eq l nil) (cons x nil))
 ((< x (car l)) (cons x l))
 (t (cons
 (car l)
 (insert x (cdr l))))))

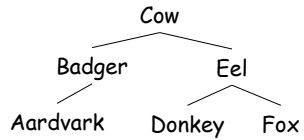
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Encoding Trees



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Encoding Trees



```
'(Cow (Badger (Aardvark nil nil) nil)
      (Eel (Donkey nil nil) (Fox nil nil)))'
```

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Encoding Records

```
class Book {
  String author;
  String title;
  int year;
  ...
}
```

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Encoding Book Records

List Form: (Author Title Year)

ex: (Melville Moby-Dick 1851)

```
(defun author (book) (car book) )
(defun title (book) (car (cdr book)) )
(defun year (book) (car (cdr (cdr book))))
```

```
(author '(Melville Moby-Dick 1851)) -> Melville
(title '(Melville Moby-Dick 1851)) -> Moby-Dick
(year '(Melville Moby-Dick 1851)) -> 1851
```

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Encoding Records

```
books: '((Joyce Ulysses 1922)
        (Melville Moby-Dick 1851)
        (McCarthy Lisp 1960)
        ...)
```

```
(titles books) -> (Moby-Dick Ulysses Lisp ..)
```

```
(years books) -> (1922 1851 1960 ..)
```

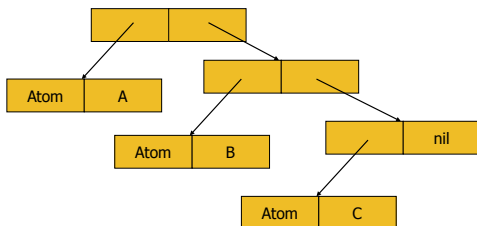
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Lisp Memory Model

- Cons cell:

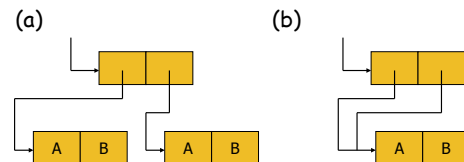
Address	Decrement
---------	-----------
- Atom:

Atom	value
------	-------
- (cons 'A (cons 'B (cons 'C nil)))



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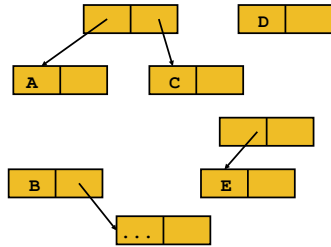
Sharing



- Both structures could be printed as (A.B).(A.B)
- Which is result of evaluating
(cons (cons 'A 'B) (cons 'A 'B)) ?

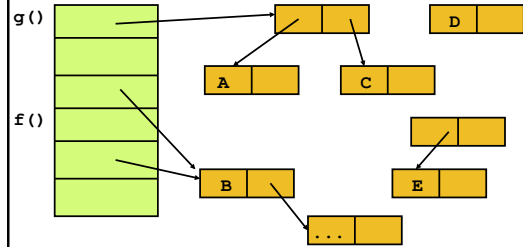
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Clear Tags



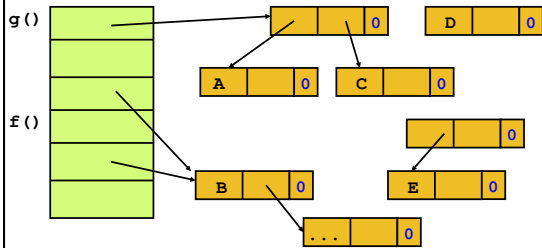
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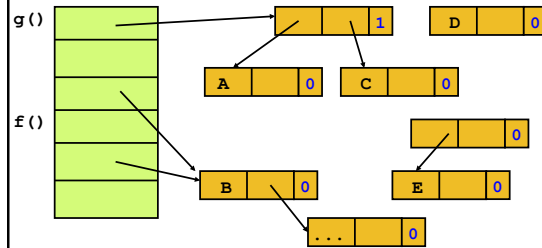
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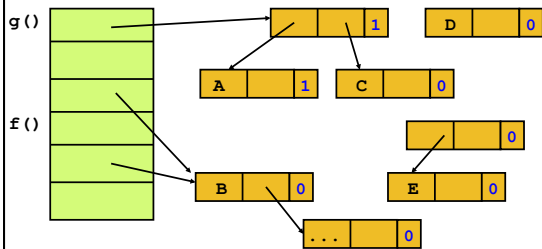
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Mark Reachable Cells



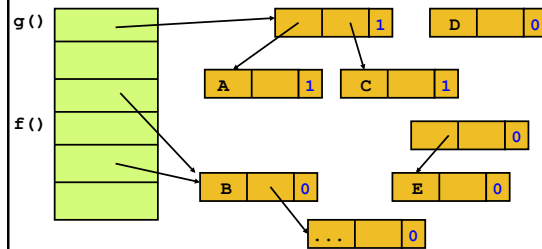
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Mark Reachable Cells



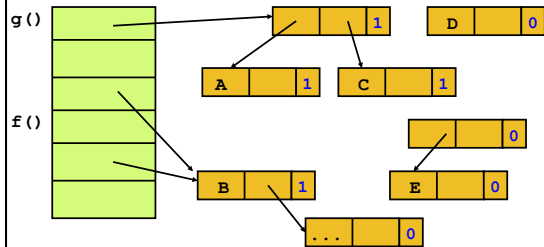
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Mark Reachable Cells



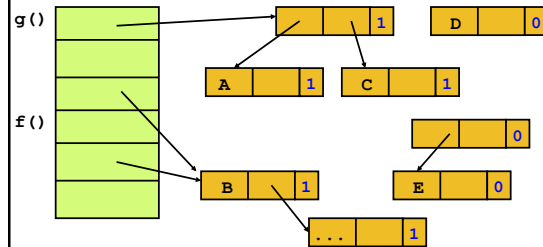
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Mark Reachable Cells



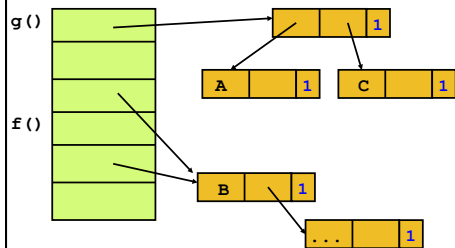
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Mark Reachable Cells



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Free Unreachable Cells



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Programs As Data

```
; substitute "to" for "from" in "term"
(defun substitute (to from term)
  (cond ((atom term)
        (cond ((eq term from) to)
              (t term)))
        (t (cons (substitute to from (car term))
                  (substitute to from (cdr term))))))

(substitute 3 'w '(+ (- 5 w) (* w w)))

is (+ (- 5 3) (* 3 3))
```

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Programs As Data

```
(defun substitute-and-eval (to from term)
  (eval (substitute to from term)))

(substitute-and-eval '* '+' (+ 10 2 3))
evaluates to 60

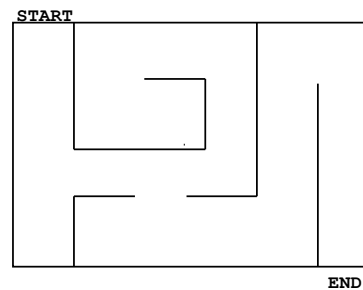
(derivative '(* 3 x x)) -> '(* 6 x)

(substitute-and-eval 6
  'x
  (derivative '(* 3 x x))) -> 36
```

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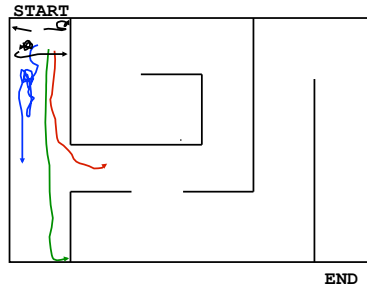
Genetic Programming

[GP Example](#)



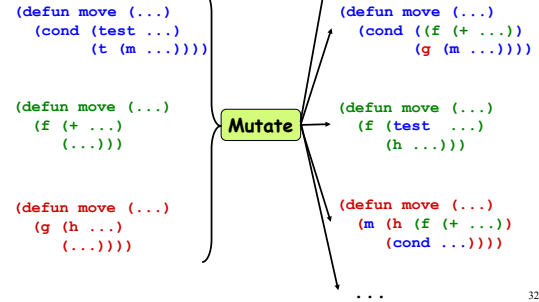
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Genetic Programming



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Genetic Programming



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