

CSCI 136

Data Structures & Advanced Programming

Lecture 17
Spring 2018
Profs Bill & Jon

Administrative Details

- Congratulations
- Lab 7: PostScript
 - Will be posted over Spring Break
 - Can't wait!?
 - Read about it in Java Structures: Section 10.5
 - No partners this time
 - Review before lab & come to lab with design doc

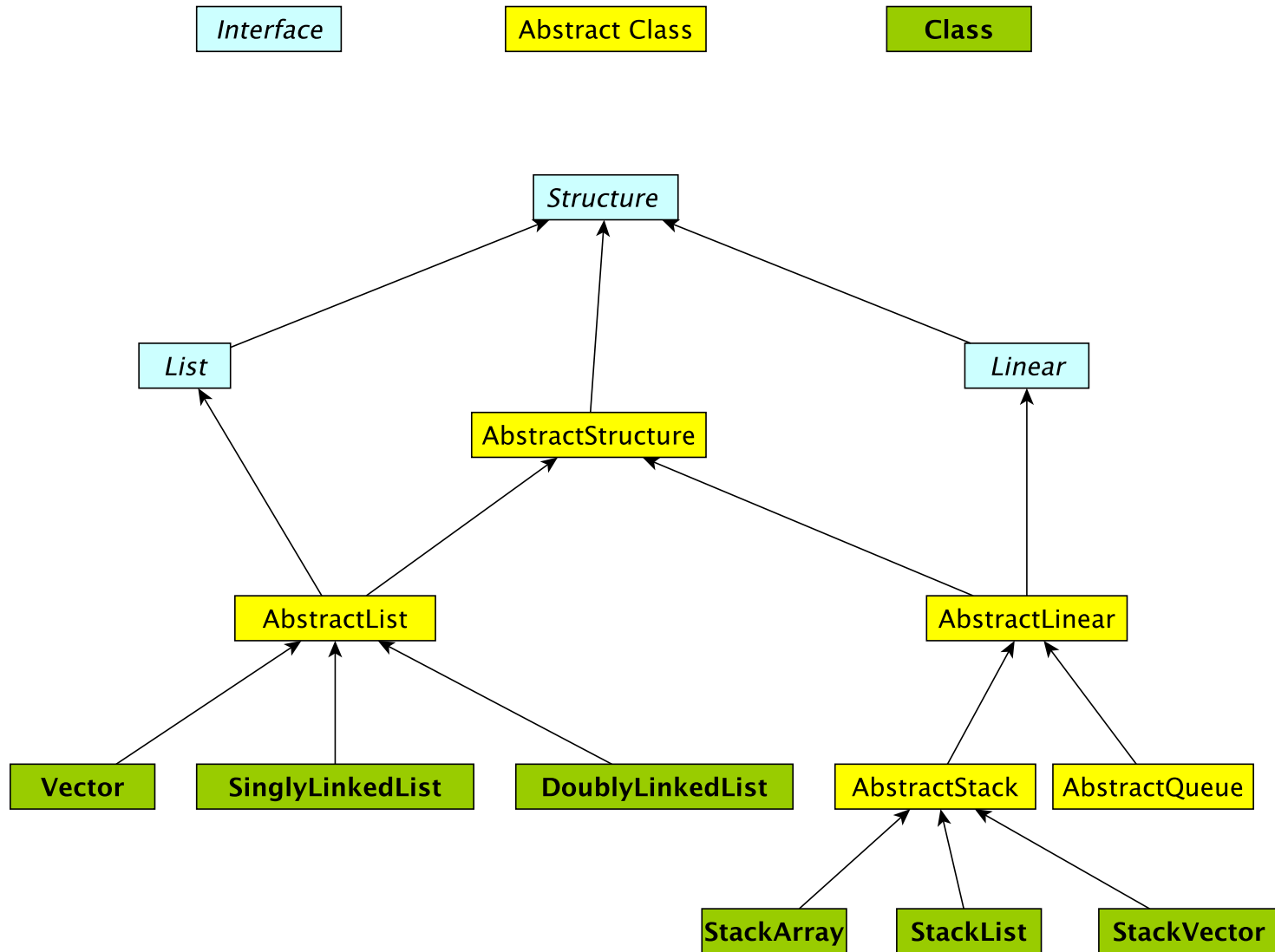
Last Time : Linear Structures

- Linear Interface
- AbstractLinear
- Stacks
 - StackArray
 - StackList
 - StackVector

Today: Linear Structures

- Stack Applications
 - Postfix expressions
 - Postscript
 - Program Stack
- Queues
 - Implementation Details
 - Applications
- Iterators

The Structure5 Universe (next)



The Linear Hierarchy

- `Linear` interface extends `Structure`
 - `add(E val)`
 - `empty()`
 - `get()`
 - `remove(),`
 - `size()`
- `AbstractLinear` (partially) implements `Linear`
- `AbstractStack` class (partially) extends `AbstractLinear`
 - Essentially introduces “stack-ish” names for methods
 - `push(E val)` is `add(E val)`
 - `pop()` is `remove()`
 - `peek()` is `get()`

Building The Hierarchy

- We extend `AbstractStack` to make “concrete” Stack types
 - `StackArray<E>`
 - holds an array of type E
 - add/remove at high end
 - `StackVector<E>`
 - Similar to `StackArray<E>`, but with a vector for dynamic growth
 - `StackList<E>`
 - A singly-linked list with add/remove at head
 - For each, we implement `add`, `empty`, `get`, `remove`, `size` directly
 - `push`, `pop`, `peek` are indirectly implemented by abstract class

Stack Applications

- The Stack implementation is simple, but there are *many* applications
 - Evaluating mathematical expressions
 - Searching (**Depth-first search**)
 - Removing recursion for optimization
 - ...



See book for details because
this is VERY useful!

Evaluating Arithmetic Expressions

- Computer programs regularly use stacks to evaluate arithmetic expressions
- Example: $x*y+z$
 - First rewrite as $xy*z+$
 - *we'll look at this rewriting process in more detail soon*
 - Then:
 - push x
 - push y
 - * (*pop twice, multiply popped items, push result*)
 - push z
 - + (*pop twice, add popped items, push result*)

Converting Expressions

- We (humans) primarily use **infix** notation to evaluate expressions
 - $(x+y)*z$
- Computers traditionally used **postfix** (also called Reverse Polish) notation
 - $xy+z*$
 - Operators appear after operands, parentheses are not necessary
- How do we convert between the two?
 - Compilers do this for us

Converting Expressions

- Example: $x*y+z*w$
- Conversion
 - 1) Add full parentheses to preserve order of operations
 $((x*y)+(z*w))$
 - 2) Move all operators (+-*/) after operands
 $((xy*)(zw*)+)$
 - 3) Remove parentheses
 $xy*zw*+$

Use Stack to Evaluate Postfix Exp

- While there are input “tokens” (i.e., symbols) left:
 - Read the next token from input.
 - If the token is a value, push it onto the stack.
 - Else, the token is an operator that takes n arguments.
 - (It is known a priori that the operator takes n arguments.)
 - If there are fewer than n values on the stack \rightarrow error.
 - Else, pop the top n values from the stack.
 - Evaluate the operator, with the values as arguments.
 - Push the returned result, if any, back onto the stack.
 - The top value on the stack is the result of the calculation.
 - Note that results can be left on stack to be used in future computations:
 - Eg: $3\ 2\ *\ 4\ +$ followed by $5\ /$ yields 2 on top of stack

Example

- $(x*y)+(z*w) \rightarrow xy*zw*+$
- Evaluate $xy*zw*+$:
 - Push x
 - Push y
 - Mult: Pop y, Pop x, Push $x*y$
 - Push z
 - Push w
 - Mult: Pop w, Pop z, Push $z*w$
 - Add: Pop $x*y$, Pop $z*w$, Push $(x*y)+(z*w)$
 - Result is now on top of stack
- Try with: $w=3, x=4, y=5, z=6$

Preview: PostScript

- PostScript is a programming language used for generating vector graphics
 - Best-known application: describing pages to printers
- It is a stack-based language
 - Values are put on stack
 - Operators pop values from stack, put result back on
 - There are numeric, logic, string values
 - Many operators
- Let's try it: The 'gs' command runs a PostScript interpreter....
- You'll be writing a (tiny part of) gs in lab soon....

Preview: PostScript

- Types: numeric, boolean, string, array, dictionary
- Operators: arithmetic, logical, graphic, ...
- Procedures
- Variables: for objects and procedures
- PostScript is just as powerful as Java, Python, ...
 - Not as intuitive
 - Easy to automatically generate
 - [RNAbows](#)

Stacks vs. Queues

- Stacks are LIFO (Last In First Out)
- Queues are FIFO (First In First Out)
 - Another linear data structure (implements `Linear` interface)
 - Queue interface methods: `enqueue` (add), `dequeue` (remove), `getFirst` (get), `peek` (get)

Queues



- Examples:
 - Lines at movie theater, grocery store, etc.
 - OS event queue (keeps keystrokes, mouse clicks, etc, in order)
 - Printers
 - Routing network traffic (more on this later)

Queue Interface

```
public interface Queue<E> extends Linear<E> {  
    public void enqueue(E item);  
    public E dequeue();  
    public E getFirst(); //value not removed  
    public E peek();    //same as get()  
}
```

Implementing Queues

As with Stacks, we have three options:

QueueArray

```
class QueueArray<E> implements Queue<E> {  
    protected Object[] data; //can't instantiate E[]  
    int head;  
    int count; // can be used to determine tail...  
}
```

QueueVector

```
class QueueVector<E> implements Queue<E> {  
    protected Vector<E> data;  
}
```

QueueList

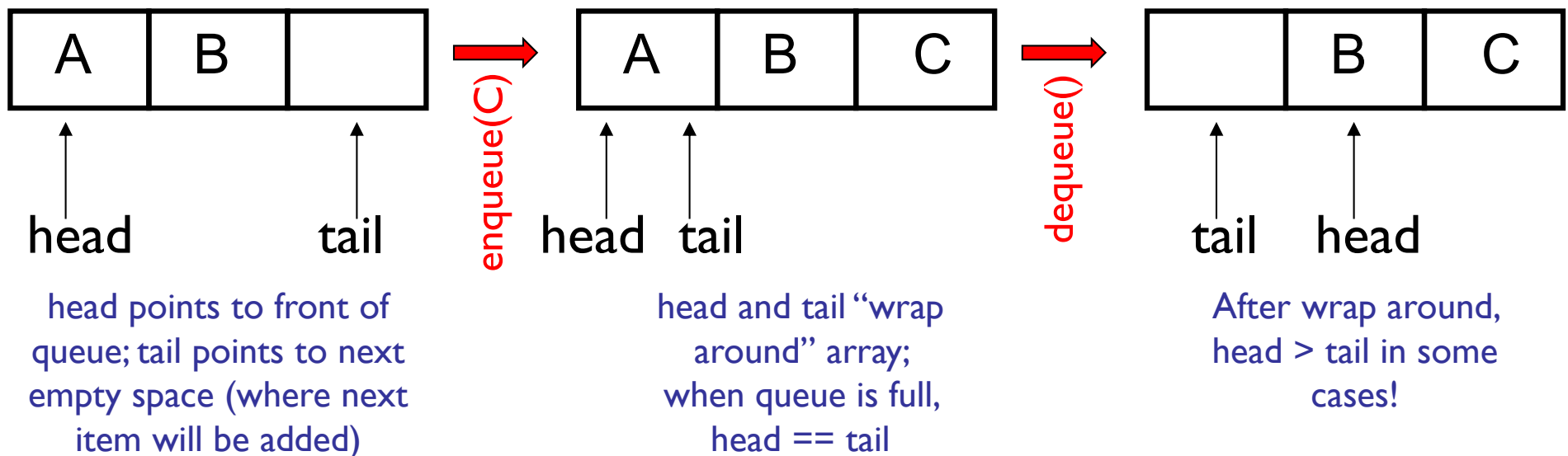
```
class QueueList<E> implements Queue<E> {  
    protected List<E> data; //uses a CircularList  
}
```

Tradeoffs:

- **QueueArray:**
 - enqueue is $O(1)$
 - dequeue is $O(1)$
 - Faster operations, but limited size
- **QueueVector:**
 - enqueue is $O(1)$ (but $O(n)$ in worst case - ensureCapacity)
 - dequeue is $O(n)$
- **QueueList:**
 - enqueue is $O(1)$ (addLast)
 - dequeue is $O(1)$ (CLL removeFirst)

QueueArray

- Let's look at an example...
- How to implement?
 - enqueue(item), dequeue(), size()



```
public class QueueArray<E> {

    protected Object[] data;          // Must use object because...
    protected int head;
    protected int count;

    public QueueArray(int size) {
        data = new Object[size]; // ... can't say "new E[size]"
    }

    public void enqueue(E item) {
        assert (count < data.length) : "The queue is full.";
        int tail = (head + count) % data.length;
        data[tail] = item;
        count++;
    }

    public E dequeue() {
        assert (count > 0) : "The queue is empty.";
        E value = (E)data[head];
        data[head] = null;
        head = (head + 1) % data.length;
        count--;
        return value;
    }

    public boolean empty() {
        return count>0;
    }
}
```