

[TAP:DMPLA] Selection Sort

```
public static void selectionSort(int[] data) {  
    for (int curN = data.length - 1; curN > 0; curN--) {  
        int maxIdx = 0;  
        for (int i = 1; i <= curN; i++) {  
            if (data[i] > data[maxIdx])  
                maxIdx = i; (compare (data.get(i), data.get(maxIdx)) > 0)  
        }  
        swap(data, maxIdx, curN);  
    }  
}  
  
public static void main(String[] args) {  
    Vector<Patient> patients;  
    ...  
    selectionSort(patients, new NameComparator());  
}
```

- What would you change if you want to sort a Vector using a Comparator (see the main method)?

- A. I'm fully sure
- B. I'm partially sure
- C. I'm not sure

Administrative Details

- Lab 5 Today
 - Submit partners!
 - Challenging, but shorter and a partner lab – more time for exam prep!
- Mid-term exam is Wednesday, March 14
 - During your normal lab session
 - You'll have approximately 1 hour & 45 minutes (if you come on time!)
 - Closed-book: Covers Chapters 1-7 & 9, handouts, and all topics up through Sorting
 - A “sample” mid-term **and** study sheet will be available online

Today's Outline

- Sort
- • Merge Sort
- Quick Sort

Sorting a Deck of Cards

Time Complexity:

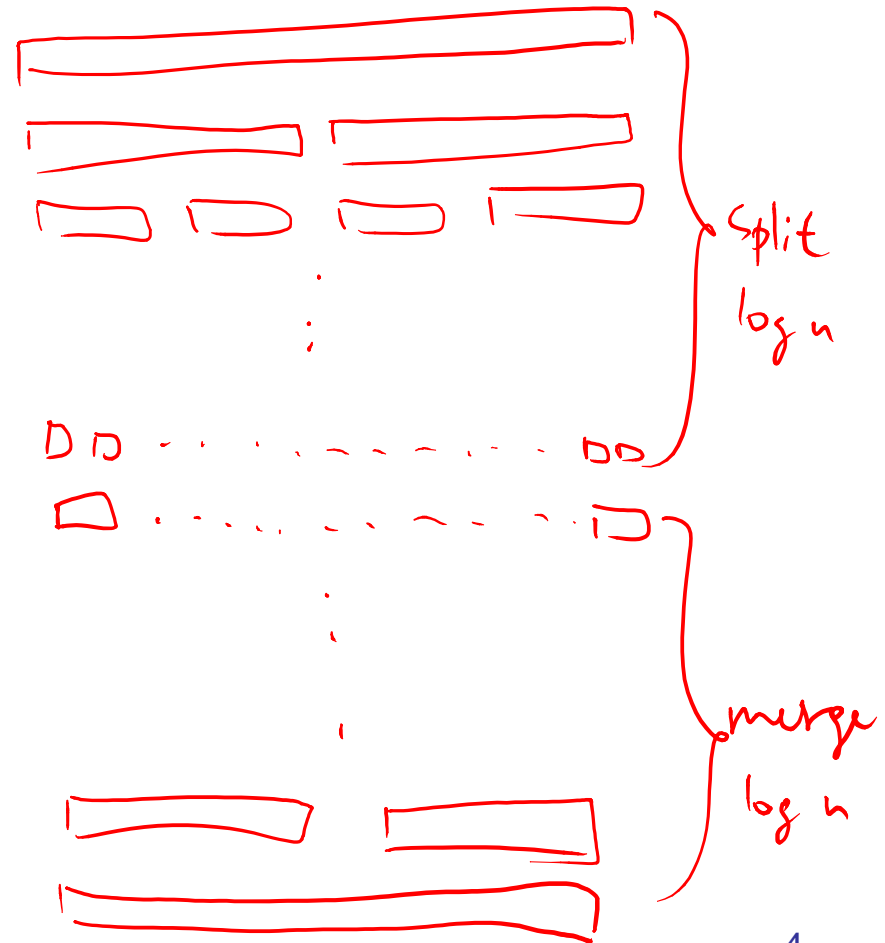
A. $O(n)$

B. $O(n \log n)$

C. $O(n^2)$

D. $O(n^3)$

E. Not sure



Merge Sort

- [8 14 29 1 17 39 16 9]
- [8 14 29 1] [17 39 16 9]
- [8 14] [29 1] [17 39] [16 9]
- [8] [14] [29] [1] [17] [39] [16] [9]
- [8 14] [1 29] [17 39] [9 16]
- [1 8 14 29] [9 16 17 39]
- [1 8 9 14 16 17 29 39]

Merge Sort



```
public static void mergeSort(int[] data) {
```

```
    int[] temp = new int[data.length];
```

```
    mergeSortHelper(data, 0, data.length - 1, temp);
```

```
}
```

```
public static void mergeSortHelper(int[] data, int low, int high) {
```

```
    // base case
```

```
    if (low >= high)
```

```
        return;
```

```
    // recursive case
```

```
    int mid = (low + high) / 2;
```

```
    mergeSortHelper(data, low, mid, temp);
```

```
    mergeSortHelper(data, mid + 1, high, temp);
```

```
    merge(data, low, mid + 1, high, temp);
```

```
}
```

Aside: merge() method

```
public static void merge(int[] data, int low, int mid, int high) int[] temp
```

```
int[] temp = new int[data.length];
```

```
int left = low;
```

```
int right = mid;
```

```
int cur = low;
```

```
while (left <= mid-1 && right <= high) {
```

```
    if (data[left] < data[right])
```

```
        temp[cur++] = data[left++];
```

```
    else
```

```
        temp[cur++] = data[right++];
```

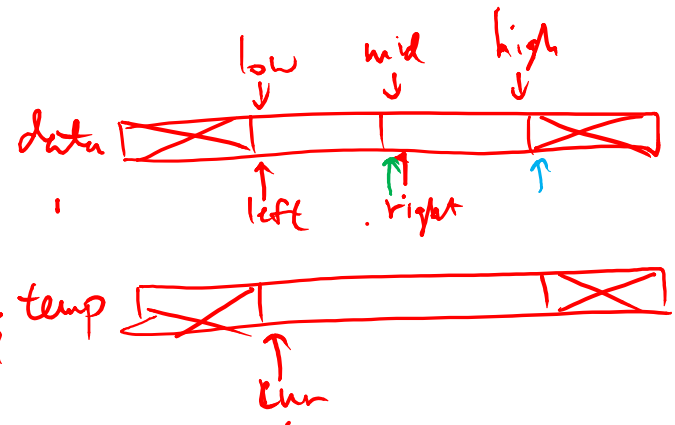
```
}
```

```
while (left <= mid-1)
```

```
    temp[cur++] = data[left++];
```

```
while (right <= high)
```

```
    temp[cur++] = data[right++];
```



```
for (int i = low; i <= high; i++)  
    data[i] = temp[i];
```

Merge Sort Summary

- Overview (A “divide and conquer” approach)
 - Recursively divide the list in half, until each sublist contains only 1 element (i.e. “sorted”)
 - Recursively (sort-)merge sorted sublists
- Time complexity:
 - Best case: $O(n \log n)$
 - Average case: $O(n \log n)$
 - Worst case: $O(n \log n)$
- Space complexity:
 - $O(2n) = O(n)$

Today's Outline

- Sort
 - Merge Sort
 - • Quick Sort

Sorting a Deck of Cards

Time Complexity:

A. $O(n)$

B. $O(n \log n)$ ← best, ave

C. $O(n^2)$ ← worst

D. $O(n^3)$

E. Not sure

Quick Sort (random pivot)

- [8 14 29 1 17 39 16 9]
 - [8 14 1 9 16 29 17 39]
 - [1 8 14 9 16 17 29 39]
 - [1 8 9 14 16 17 29 39]
- } $\approx \log n$
(n in the worst case)

Quick Sort (pivot = left-most element)

- [8 14 29 1 17 39 16 9]
- [1 **8** 14 29 17 39 16 9]
- [1 **8** 9 **14** 29 17 39 16]
- [1 **8** 9 **14** 16 17 **29** 39]
- [1 **8** 9 **14** **16** 17 **29** 39]

Quick Sort

```
public static void quickSort(int[] data) {
```

```
    quickSortHelper(data, 0, data.length - 1);
```

```
}
```

```
public static void quickSortHelper(int[] data, int low, int high) {
```

```
    // base case
```

```
    if (low >= high)
```

```
        return;
```

```
    // recursive case
```

```
    int pivotI = partition(data, low, high);
```

```
    quickSortHelper(data, low, pivotI);
```

```
    quickSortHelper(data, pivotI + 1, high);
```

```
}
```

Merge Sort



```
public static void mergeSort(int[] data) {
```

```
    mergeSortHelper(data, 0, data.length - 1);
```

```
} public static void mergeSortHelper(int[] data, int low, int high) {
```

```
    // base case
```

```
    if (low >= high)
```

```
        return;
```

```
    // recursive case
```

```
    int mid = (low + high) / 2;
```

```
    mergeSortHelper(data, low, mid);
```

```
    mergeSortHelper(data, mid + 1, high);
```

```
    merge(data, low, mid + 1, high);
```

```
}
```

Aside: Partition() method

```
public static int partition(int data[], int left, int right)
```

```
int pivot = data[left];
```

```
left++;
```

```
while (left <= right) {
```

```
    if (data[left] > pivot) {
```

```
        swap(data, left, right);
```

```
        right--;
```

```
    } else {
```

```
        data[left-1] = data[left];
```

```
        left++;
```

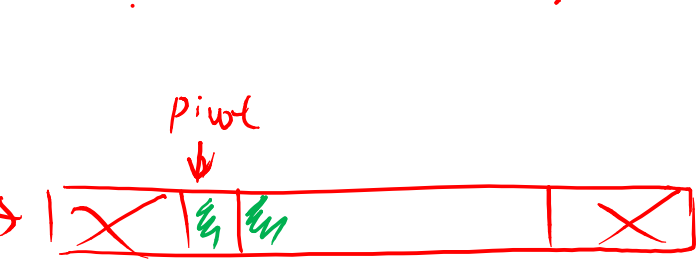
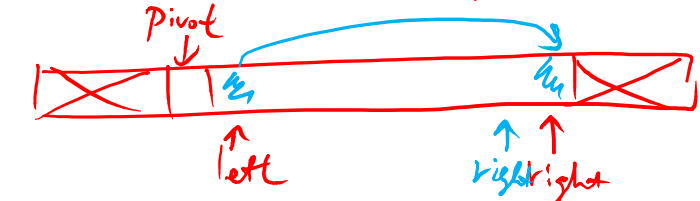
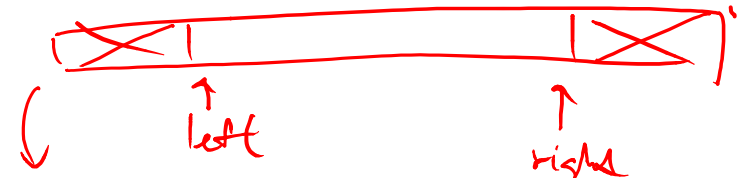
```
    }
```

```
}
```

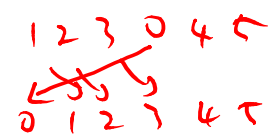
```
data[right] = pivot;
```

```
return right;
```

```
}
```



similar to insertion sort



Quick Sort Summary

- Overview
 - Randomly pick a pivot, then move smaller elements to the left and bigger to the right.
 - Recursively sort left and right sublists
- Time complexity:
 - Best case: $O(n \log n)$
 - Average case: $O(n \log n)$
 - Worst case: $O(n^2)$
- Space complexity:
 - $O(n)$

Sorting : Time Complexity

Algorithm	Best	Ave	Worst
Bubble	$O(n)$	$O(n^2)$	$O(n^2)$
Selection	$O(n^2)$	$O(n^2)$	$O(n^2)$
Insertion	$O(n)$	$O(n^2)$	$O(n^2)$
Merge	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Quick	$O(n \log n)$	$O(n \log n)$	$O(n^2)$