

Balance

cs136

Review

- A **balanced** binary search tree implements all core operations in $O(\lg n)$
- Binary search trees are typically used as **maps** (Dictionaries)
 - Ordered (comparable) **key**
 - Used to reference a **value**
- BST insert, contains, get, and remove have common code...**locate()** helper
- Depth-first in-order iteration gives the values in sorted order!
- **AVL** and **Red-Black Trees** auto-balance
- **Splay Trees** don't maintain balance...but still give expected, amortized $O(\lg n)$

Splay Tree Demonstration



Self-adjusting binary search trees

Sleator and Tarjan

Journal of the ACM, 1985

<https://github.com/morgan3d/misc/tree/master/splaytree>

Implementing Balance()

- Depth-first in-order iteration gives the values in sorted order
- Inserting in "binary search order" from a sorted array gives a balanced BST
- Strategy:
 - Extract sorted array of elements from an arbitrary BST
 - Clear the tree
 - Insert via "depth first" iteration on the *array*
- Warmup:
 - Look at print()
 - Implement printSorted()

Summary

- Easy to implement code to balance a BST!
- Recursion is beautiful
- Exciting conclusion on Monday: `BST.remove()`