

HEAP SORT

CS136

RETURN TO BINARY TREES

Monday: Heap sort

Wednesday: BST implementation

Friday: BST balance

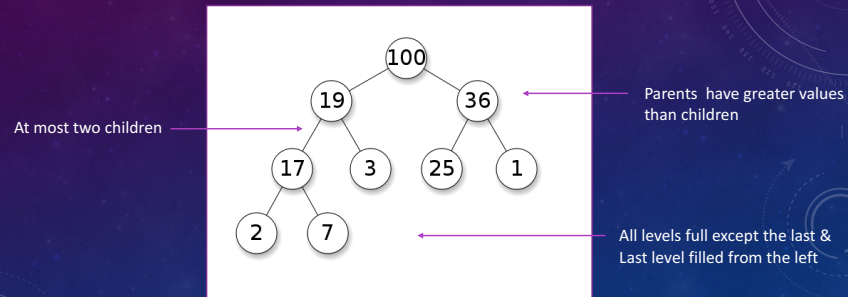
Monday: BST remove

HEAP SORT

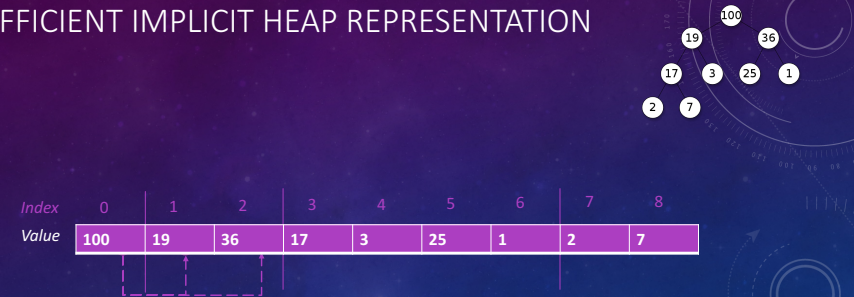
- Deterministic, but not stable
- $O(n \lg n)$ run time
- Only $O(1)$ additional cost!
 - Works in place
 - Stackless
- Ideal for fixed-memory environments, like GPU kernel programming and embedded processors
 - Faster than insertion sort, and merge and quicksort are impossible in this environment
- Elegant implementation

HEAP REVIEW

HEAP = COMPLETE BINARY TREE WITH HEAP PROPERTY



EFFICIENT IMPLICIT HEAP REPRESENTATION



HEAP SORT IMPLEMENTATION

HEAP SORT IDEA

- Build a **max heap** using the **implicit complete** binary tree notation
 - Children of node at i are at $2i+1$ and $2i+2$
 - Parent is greater than its children (and has index $\text{floor}((i-1)/2)$)
 - Repeated "sift down" operations
- Repeatedly extract the **max**
 - On step j , swap element 0 with element $N - j - 1$
 - Consider the end fixed and **sift down** the new root

BE CAREFUL

- The tree is a *concept*
 - No explicit tree
 - No pointers
- The heap structure is *not* itself sorted
- We build a *max* heap to sort from least to greatest because we're going to read the values out in backwards order

```
public class HeapSort {
    /* Helper function: sift element[parent] down the tree */
    void siftDown(Element[] element, int parent, final int end) {
        final Element value = element[parent];
        int maxChild = parent * 2 + 1;
        while (maxChild <= end) {
            // See if the other child is larger
            if (maxChild < end) {
                final int otherChild = maxChild + 1;
                maxChild = (element[otherChild] > element[maxChild]) ?
                    otherChild : maxChild;
            }
            // Stop when the parent is larger than the max child
            if (value >= element[maxChild]) break;
            element[parent] = element[maxChild];
            parent = maxChild;
            maxChild = parent * 2 + 1;
        }
        element[parent] = value;
    }

    public void heapSort(Element[] element) {
        // Form a max heap
        final int N = element.length;
        for (int i = N / 2; i >= 0; --i)
            siftDown(element, i, N - 1);
        // Read out the values
        for (int i = N - 1; i >= 1; --i) {
            // Swap out of the heap region
            final Element temp = element[0];
            element[0] = element[i];
            element[i] = temp;
            // Restore the heap property
            siftDown(element, 0, i - 1);
        }
    }
}
```