CSCI 136 Data Structures & Advanced Programming

> Lecture 14 Fall 2018 Instructor: Bills

Announcements

- Mid-Term Review Session
 - Monday (10/15), 7:00-8:00 pm in TPL 203
 - No prepared remarks, so bring questions!
- Mid-term exam is Wednesday, October 17
 - During your normal lab session
 - You'll have I hour & 45 minutes (if you come on time!)
 - Closed-book
 - Covers Chapters 1-7 & 9 and all topics up through Linked Lists
 - A "sample" mid-term and study sheet are available online
 - See Handouts & Problem Sets

Last Time

- QuickSort and Sorting Wrap-Up
- Linear Structures
 - The Linear Interface (LIFO & FIFO)
 - The AbstractLinear and AbstractStack classes
- Stack Implementations
 - StackArray, StackVector, StackList,

Today: Linear Structures

- Stack applications
 - Expression Evaluation
 - PostScript: Page Description & Programming
 - Mazerunning (Depth-First-Search)

Evaluating Arithmetic Expressions

- Computer programs regularly use stacks to evaluate arithmetic expressions
- Example: x*y+z
 - First rewrite as xy*z+ (we'll look at this rewriting process in more detail soon)
 - Then:
 - push x
 - push y
 - * (pop twice, multiply popped items, push result)
 - push z
 - + (pop twice, add popped items, push result)

Converting Expressions

- We (humans) primarily use "infix" notation to evaluate expressions
 - (x+y)*z
- Computers traditionally used "postfix" (also called Reverse Polish) notation
 - xy+z*
 - Operators appear after operands, parentheses not necessary
- How do we convert between the two?
 - Compilers do this for us

Converting Expressions

- Example: x*y+z*w
- Conversion
 - Add full parentheses to preserve order of operations ((x*y)+(z*w))
 - Move all operators (+-*/) after operands ((xy*)(zw*)+)
 - 3) Remove parentheses

xy*zw*+

Use Stack to Evaluate Postfix Exp

- While there are input "tokens" (i.e., symbols) left:
 - Read the next token from input.
 - If the token is a value, push it onto the stack.
 - Else, the token is an operator that takes n arguments.
 - (It is known a priori that the operator takes n arguments.)
 - If there are fewer than n values on the stack \rightarrow error.
 - Else, pop the top n values from the stack.
 - Evaluate the operator, with the values as arguments.
 - Push the returned result, if any, back onto the stack.
 - The top value on the stack is the result of the calculation.
 - Note that results can be left on stack to be used in future computations:
 - Eg: 3 2 * 4 + followed by 5 / yields 2 on top of stack

Example

- (x^*y) + $(z^*w) \rightarrow xy^*zw^*$ +
- Evaluate:
 - Push x
 - Push y
 - Mult: Pop y, Pop x, Push x*y
 - Push z
 - Push w
 - Mult: Pop w, Pop z, Push z*w
 - Add: Pop x*y, Pop z*w, Push (x*y)+(z*w)
 - Result is now on top of stack

Lab Preview: PostScript

- PostScript is a programming language used for generating vector graphics
 - Best-known application: describing pages to printers
- It is a stack-based language
 - Values are put on stack
 - Operators pop values from stack, put result back on
 - There are numeric, logic, string values
 - Many operators
- Let's try it: The 'gs' command runs a PostScript interpreter....
- You'll be writing a (tiny part of) gs in lab soon....

Lab Preview: PostScript

- Types: numeric, boolean, string, array, dictionary
- Operators: arithmetic, logical, graphic, ...
- Procedures
- Variables: for objects and procedures
- PostScript is just as powerful as Java, Python, ...
 - Not as intuitive
 - Easy to automatically generate
- Example: Recursive factorial procedure /fact { dup 1 gt { dup 1 sub fact mul } if } def
- Example: Drawing (see picture.ps)

Mazes

- How can we use a stack to solve a maze?
 - <u>http://www.primaryobjects.com/maze/</u>
- Properties of mazes:
 - We model a maze as a rectangular grid of cells
 - There is a start cell and one or more finish cells
 - Goal: Find path of *adjacent* free cells from *start* to *finish*
- Strategy: Consider unvisited cells as "potential tasks"
 - Use linear structure (stack) to keep track of current path being explored

Solving Mazes

- We'll use two objects to solve our maze:
 - Position: Info about a single cell
 - Maze: Grid of Positions
- General strategy:
 - Use stack to keep track of path from start
 - If we hit a dead end, backtrack by popping location off stack
 - Mark discarded cells to make sure we don't visit the same paths twice

Backtracking Search

- Try one way (favor north and east)
- If we get stuck, go back and try a different way
- We will eventually either find a solution or exhaust all possibilities
- Also called a "depth first search"

 Lots of other algorithms that we will not explore: <u>http://www.astrolog.org/labyrnth/algrithm.htm</u>

A "Pseudo-Code" Sketch

// Initialization

Read cell data (free/blocked/start/finish) from file data Mark all free cells as unvisited Create an empty stack S Mark start cell as visited and push it onto stack S

While (S isn't empty && top of S isn't finish cell) current ← S.peek() // current is top of stack If (current has an unvisited neighbor x) Mark x as visited; S.push(x) // x is explored next Else S.pop() If finish is on top of S then success else no solution

Is Pseudo-Code Correct?

- Tools
 - Concepts: adjacent cells; path; simple path; path length; shortest path; distance between cells; reachable from cell
 - Solving a maze: is *finish* reachable from *start*?
- Theorem: The pseudo-code will either visit finish or visit every free cell reachable from start
- **Proof:** Prove that if algorithm does *not* visit *finish* then it *does* visit every free cell reachable from *start*
 - Do this by induction on distance of free cell from start
 - Base case: distance 0. Easy
 - Induction: Assume every reachable free cell of distance at most k ≥ ○ from start is visited. Prove for k+l

Is Pseudo-Code Correct?

- Induction Hyp: Assume every reachable free cell of distance at most k ≥ ○ from start is visited.
- Induction Step: Prove that every reachable free cell of distance k+1 from start is visited.
 - Let c be a free cell of distance k+1 reachable from start
 - Then c has a free neighbor d that is distance k from start and reachable from start
 - But then by induction, d is visited, so it was put on stack
 - So each free neighbor of *d* is visited by algorithm
- Done!

Recursive "Pseudo-Code" Sketch

Boolean RecSolve(Maze m, Position current) If (current eqauls finish) return true Mark current as visited next ← some unvisited neighbor of current (or null if none left) While (next does not equal null & recSolve(m, next) is false) next ← some unvisited neighbor of current(or null if none left) Return next ≠ null

- To solve maze, call: *Boolean recSolve(*m, start)
- To prove correct: Induction on distance from *current* to *finish*
- How could we generate the actual solution?

Implementing A Maze Solver

- Iteratively: Maze.java
- Recursively: RecMaze.java
 - Recursive method keeps an implicit stack
 - The method call stack
 - Each recursive call adds to the stack

Implementation: Position class

- Represent position in maze as (x,y) coordinate
- class Position has several relevant methods:
 - Find a neighbor
 - Position getNorth(), getSouth(), getEast(), getWest()
 - boolean equals()
 - Check states of position
 - boolean isVisited(), isOpen()
 - Set states of position
 - void visit(), setOpen(boolean b)

Maze class

Relevant Maze methods:

- Maze(String filename)
 - Constructor; takes file describing maze as input
- void visit(Position p)
 - Visit position p in maze
- boolean isVisited(Position p)
 - Returns true iff p has been visited before
- Position start(), finish()
 - Return start /finish positions
- Position nextAdjacent(Position p)
 - Return next unvisited neighbor of p---or null if none
- boolean isClear(Position p)
 - Returns true iff p is a valid move and is not a wall

Method Call Stacks

- In JVM, need to keep track of method calls
- JVM maintains stack of method invocations (called frames)
- Stack of frames
 - Receiver object, parameters, local variables
- On method call
 - Push new frame, fill in parameters, run code
- Exceptions print out stack
- Example: StackEx.java
- Recursive calls recurse too far: StackOverflowException
 - Overflow.java

Recursive Call Stacks

```
public static long factorial(int n) {
    if (n <= 1) // base case
        return 1;
    else
        return n * factorial(n - 1);
}</pre>
```

public static void main(String args[]) {
 System.out.println(factorial(3)};
}