CSCI 136 Data Structures & Advanced Programming

> Lecture 26 Fall 2017 Instructors: Bill<<1

Administrative Details

- Lab 10: Two Towers is online
 - No partners this week!
- Final Exam location: TBL 112
 - Old news: It's on Dec. 14th, 9:30--noon

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Last Time

- Efficient Binary search trees (Ch 14)
 - AVL Trees
 - Height is O(log n), so all operations are O(log n)
 - Red-Black Trees
 - Different height-balancing idea: height is O(log n)
 - All operations are O(log n)
 - Splay Trees
 - No guaranteed balance; good *amortized* performance
 - Any sequence of m operations take O(m log n) time

Today's Outline

Less esoteric...

- Bit operations
 - Useful in general and required for Lab 10
- Introduction To Graphs
 - Basic Definitions and Properties
 - Applications and Problems

Representing Numbers

- Humans usually think of numbers in base 10
- But even though we write int x = 23; the computer stores x as a sequence of 1s and 0s
- Recall Lab 3: public static String printInBinary(int n) { if (n <= 1) return "" + n%2; return printInBinary(n/2)+n%2;
- 0000000 0000000 0000000 00010111

}

Bitwise Operations

- We can use *bitwise* operations to manipulate the 1s and 0s in the binary representation
 - Bitwise 'and': &
 - Bitwise 'or':
- Also useful: bit shifts
 - Bit shift left: <<
 - Bit shift right: >>

& and |

- Given two integers a and b, the bitwise or expression a | b returns an integer s.t.
 - At each bit position, the result has a 1 if that bit position had a 1 in EITHER a OR b (or both)

- Given two integers a and b, the bitwise and expression a & b returns an integer s.t.
 - At each bit position, the result has a 1 if that bit position had a 1 in BOTH a AND b

>> and <<

- Given two integers a and i, the expression (a << i) returns (a * 2ⁱ)
 - Why? It shifts all bits left by i positions
 - 1 << 4 = ?
- Given two integers a and i, the expression
 (a >> i) returns (a / 2ⁱ)
 - Why? It shifts all bits right by i positions
 - 1 >> 4 = ?
 - 97 >> 3 = ? (97 = 1100001)
- Be careful about shifting left and "overflow"!!!

Revisiting printlnBinary(int n)

 How would we rewrite a recursive printInBinary using bit shifts and bitwise operations?

```
public static String printInBinary(int n) {
    if (n <= 1) {
        return "" + n;
        return printInBinary(n >> 1) + (n & 1);
}
```

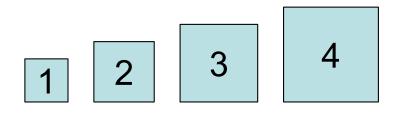
Revisiting printlnBinary(int n)

 How would we write an iterative printInBinary using bit shifts and bitwise operations?

```
String result = "";
for(int i = 0; i < width; i++)
    if ((n & (1<<i)) == 0)
        result = 0 + result;
    else
        result = 1 + result;
return result;</pre>
```

Lab 8: Two Towers

• Goal: given a set of blocks, iterate through all possible subsets to find the best set

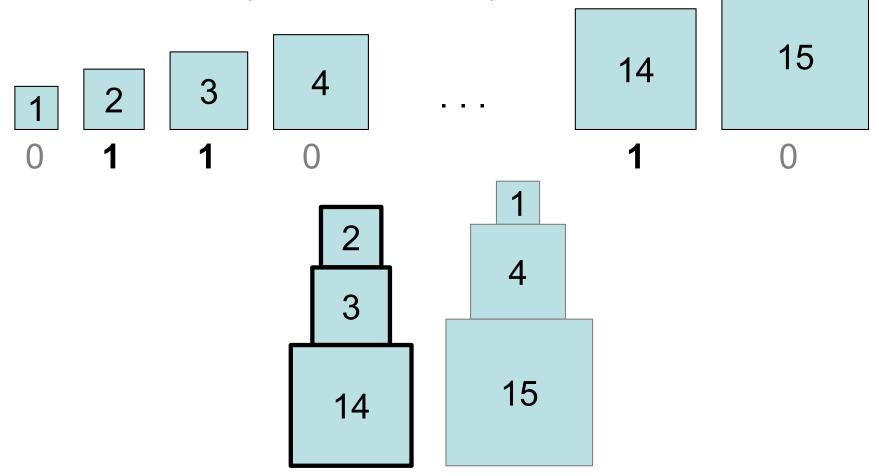


| 14 | 15 |
|----|----|
|----|----|

- "Best" set produces the most balanced towers
- Strategy: create an iterator that uses the bits in a binary number to represent subsets

Lab 8: Two Towers

- A block can either be in the set or out
 - If bit is a 1, in. If bit is a 0, out



Questions?

- We will write a "SubsetIterator" to enumerate all possible subsets of a Vector<E>
- We will use SubsetIterator to solve two problems
 - Two Towers
 - Identify all Subsequences of a String that are words
 - Use your LexiconTrie! (or an OrderedStructure)

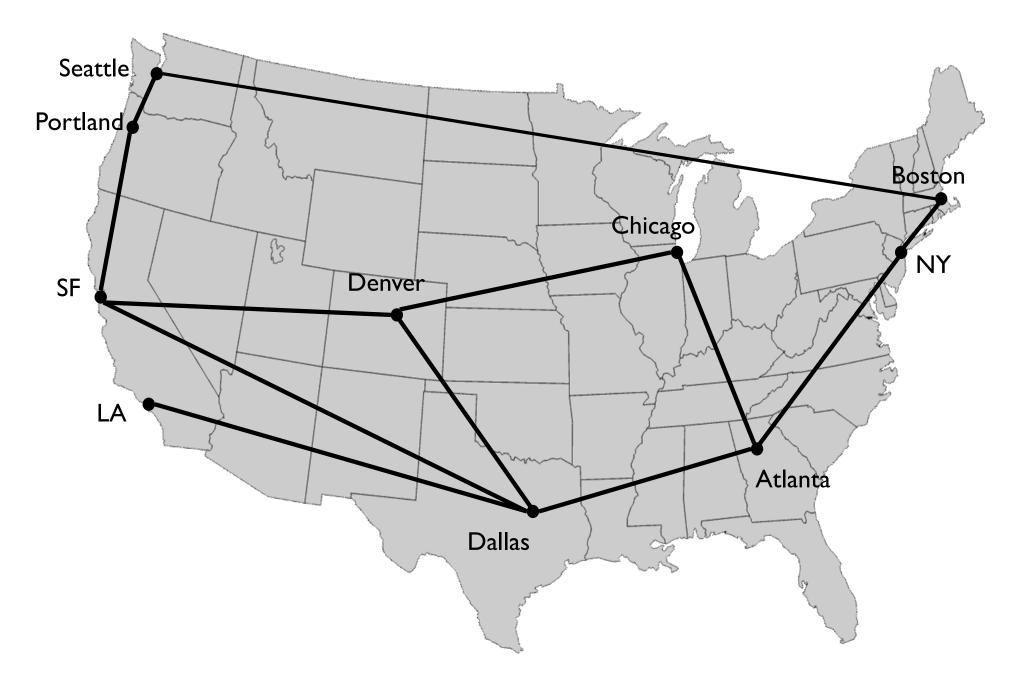
Graphs Describe the World¹

- Transportation Networks
- Communication Networks
- Molecular structures
- Dependency structures
- Scheduling
- Matching
- Graphics Modeling

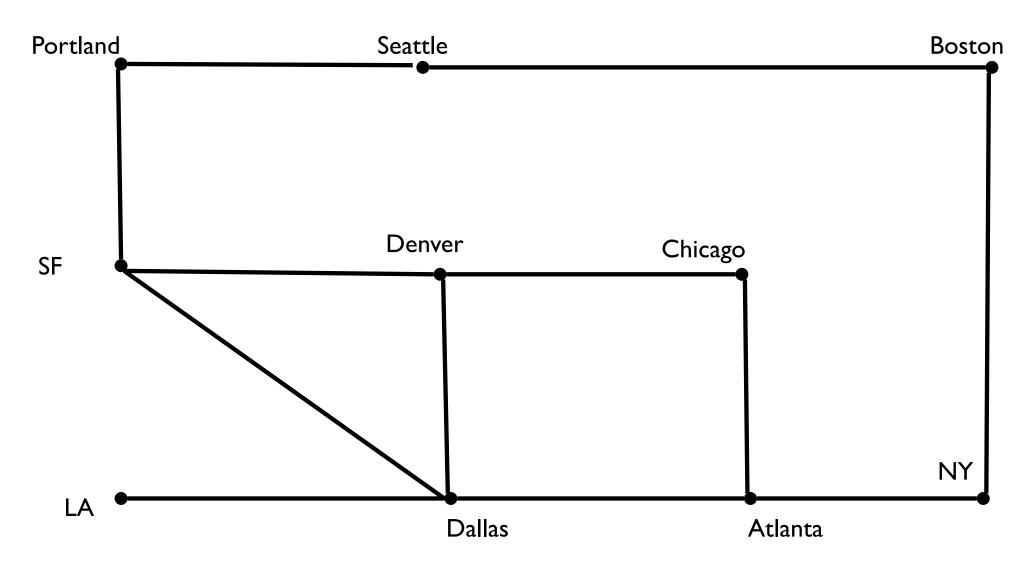
¹But don't tell Tom Garrity---he'll just be sad....



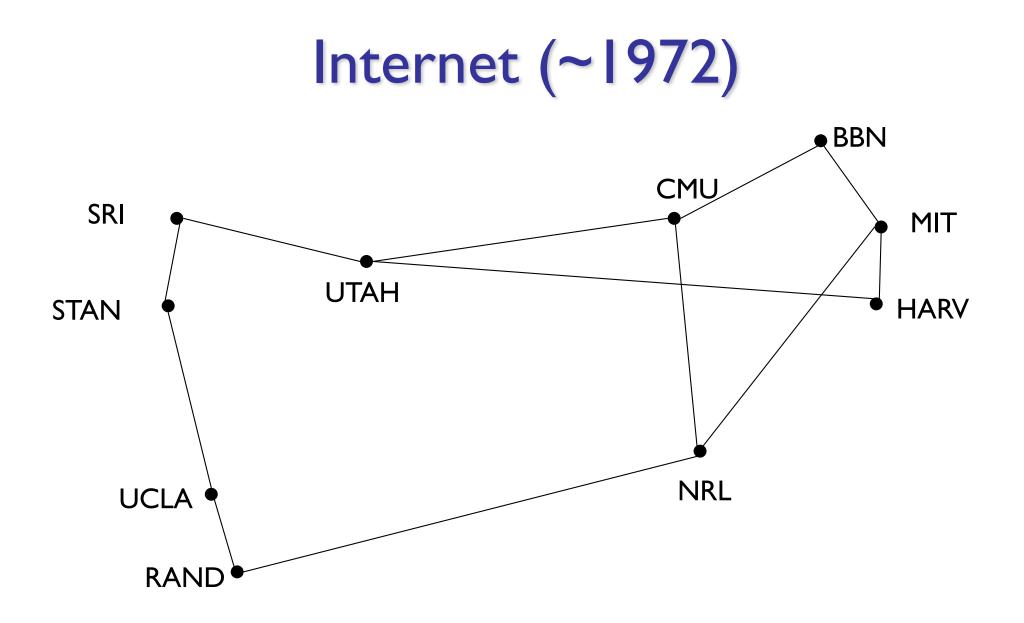
Nodes = subway stops; Edges = track between stops



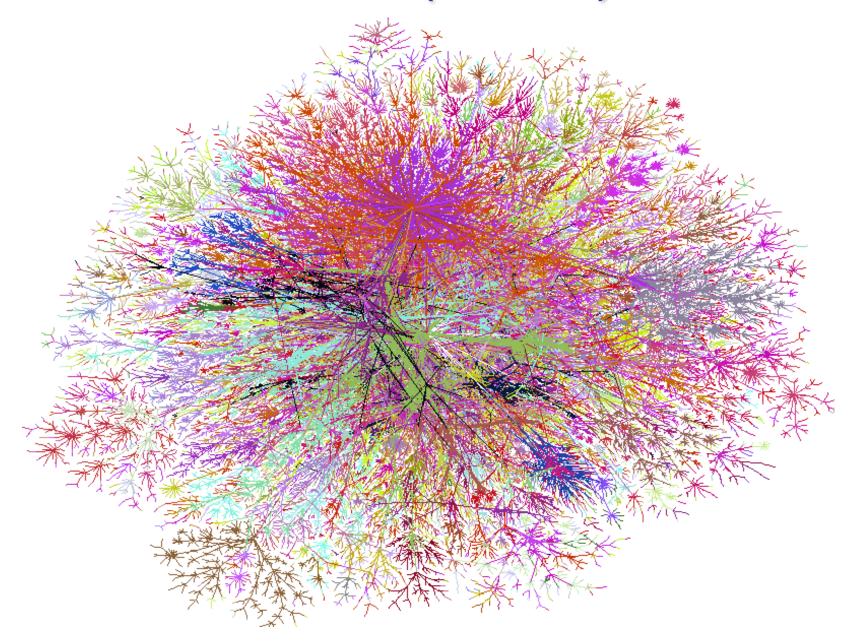
Nodes = cities; Edges = rail lines connecting cities



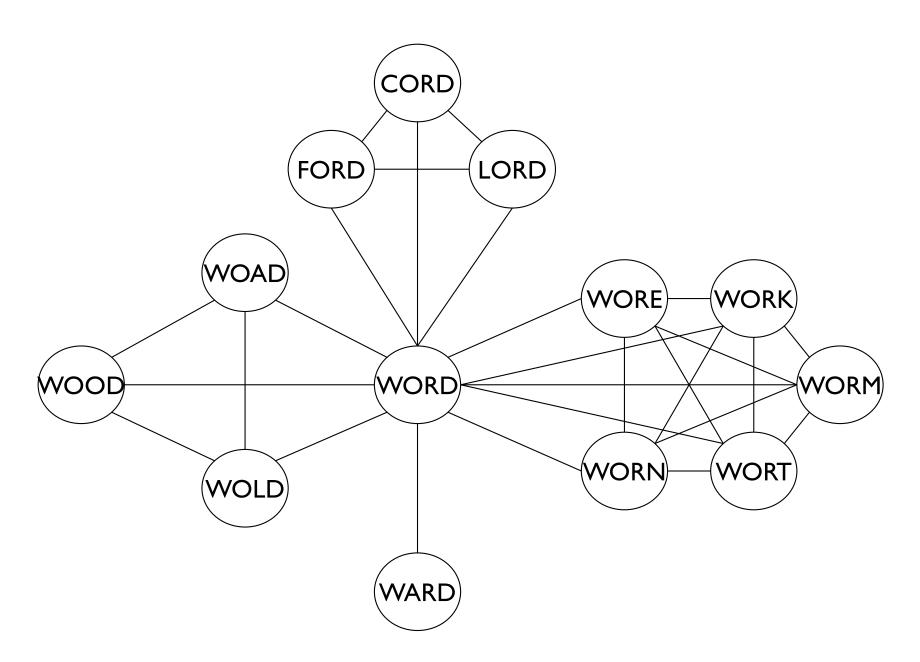
Note: Connections in graph matter, not precise locations of nodes



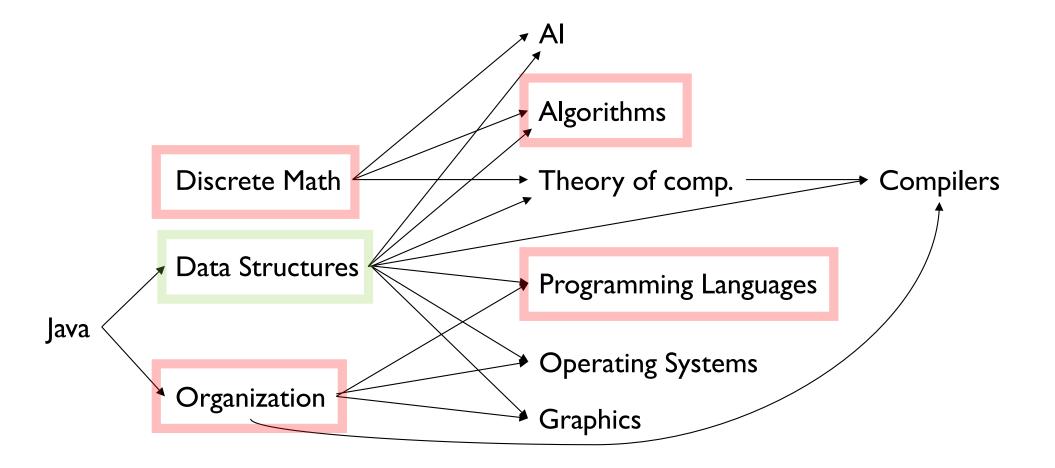
Internet (~1998)



Word Game

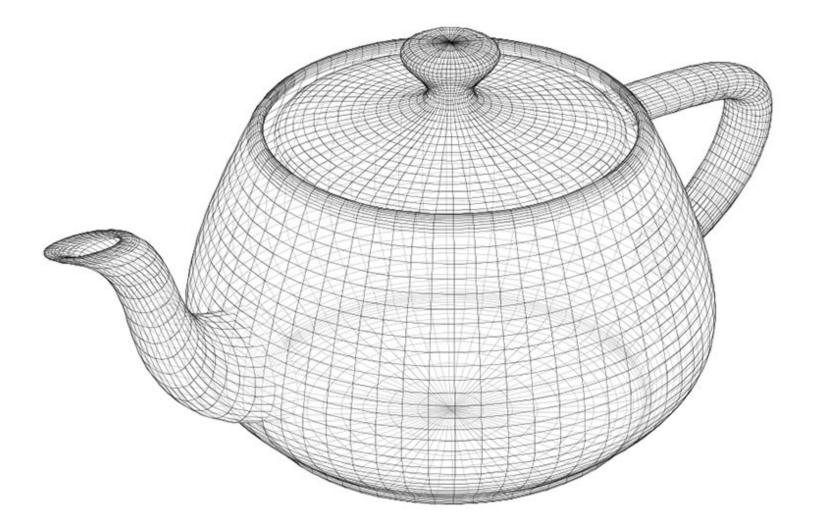


CS Pre-requisite Structure (subset)

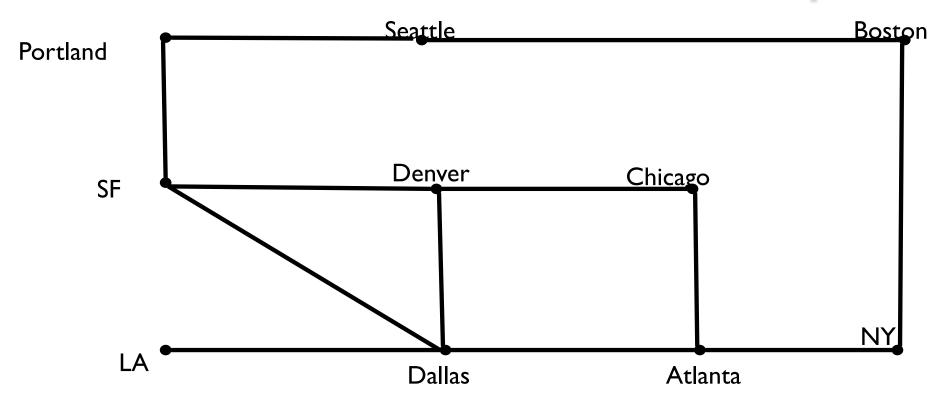


Nodes = courses; Edges = prerequisites ***

Wire-Frame Models



Basic Definitions & Concepts



Def'n: An undirected graph G = (V,E) consists of two sets

•V : the vertices of G, and E : the edges of G

•Each edge e in E is defined by a set of two vertices: its *incident* vertices. We write $e = \{u,v\}$ and say that u and v are *adjacent*.

Walking Along a Graph

 A walk from u to v in a graph G = (V,E) is an alternating sequence of vertices and edges

 $u = v_0, e_1, v_1, e_2, v_2, ..., v_{k-1}, e_k, v_k = v$

such that each $e_i = \{v_i, v_{i+1}\}$ for i = 1, ..., k

- Note a walk starts and ends on a vertex
- If no edge appears more than once then the walk is called a *path*
- If no vertex appears more than once then the walk is a simple path

Walking In Circles

• A closed walk in a graph G = (V,E) is a walk

$$v_0, e_1, v_1, e_2, v_2, \dots, v_{k-1}, e_k, v_k$$

such that each $v_0 = v_k$

- A circuit is a path where v₀ = v_k
 No repeated edges
- A cycle is a simple path where v₀ = v_k
 No repeated vertices
- The length of any of these is the number of edges in the sequence

Little Tiny Theorems

- If there is a walk from u to v, then there is a walk from v to u.
- If there is a walk from u to v, then there is a path from u to v (and from v to u)
- If there is a path from u to v, then there is a simple path from u to v (and v to u)
- Every circuit through v contains a cycle through v
- Not every closed walk through v contains a cycle through v! [Try to find an example!]