CSCI 136 Data Structures & Advanced Programming

> Lecture 15 Fall 2017 Instructor: Bills

#### Announcements

- Mid-Term Review Session
  - Tonight (10/16), 8:00-9:00 pm in TPL 205
    - And Tuesday night---same time, same place
  - No prepared remarks, so bring questions!
- Mid-term exam is Wednesday, October 18
  - During your normal lab session
  - You'll have I hour & 45 minutes (if you come on time!)
  - Closed-book
  - Covers Chapters I-7 & 9 and all topics up through sorting
  - A "sample" mid-term and study sheet are available online
    - <u>See Handouts & Problem Sets</u>

### Last Time

- QuickSort and Sorting Wrap-Up
- Linear Structures
  - The Linear Interface (LIFO & FIFO)
  - The AbstractLinear and AbstractStack classes
- Stack Implementations
  - StackArray, StackVector, StackList,
- Stack applications
  - Expression Evaluation
  - PostScript: Page Description & Programming

# **Today: Linear Structures**

- Stack applications
  - A Bit More PostScript
  - Mazerunning (Depth-First-Search)
- Queues
  - Implementations
  - Applications

## **Converting Expressions**

- We (humans) primarily use "infix" notation to evaluate expressions
  - (x+y)\*z
- Computers traditionally used "postfix" (also called Reverse Polish) notation
  - xy+z\*
  - Operators appear after operands, parentheses not necessary
- How do we convert between the two?
  - Compilers do this for us

## **Converting Expressions**

- Example: x\*y+z\*w
- Conversion
  - Add full parentheses to preserve order of operations ((x\*y)+(z\*w))
  - Move all operators (+-\*/) after operands ((xy\*)(zw\*)+)
  - Remove parentheses
     xy\*zw\*+

### Use Stack to Evaluate Postfix Exp

- While there are input "tokens" (i.e., symbols) left:
  - Read the next token from input.
  - If the token is a value, push it onto the stack.
  - Else, the token is an operator that takes n arguments.
    - (It is known a priori that the operator takes n arguments.)
    - If there are fewer than n values on the stack  $\rightarrow$  error.
    - Else, pop the top n values from the stack.
      - Evaluate the operator, with the values as arguments.
      - Push the returned result, if any, back onto the stack.
  - The top value on the stack is the result of the calculation.
  - Note that results can be left on stack to be used in future computations:
    - Eg: 3 2 \* 4 + followed by 5 / yields 2 on top of stack

# Example

- $(x^*y)$ + $(z^*w) \rightarrow xy^*zw^*$ +
- Evaluate:
  - Push x
  - Push y
  - Mult: Pop y, Pop x, Push x\*y
  - Push z
  - Push w
  - Mult: Pop w, Pop z, Push z\*w
  - Add: Pop x\*y, Pop z\*w, Push (x\*y)+(z\*w)
  - Result is now on top of stack

#### Preview: PostScript

- PostScript is a programming language used for generating vector graphics
  - Best-known application: describing pages to printers
- It is a stack-based language
  - Values are put on stack
  - Operators pop values from stack, put result back on
  - There are numeric, logic, string values
  - Many operators
- Let's try it: The 'gs' command runs a PostScript interpreter....
- You'll be writing a (tiny part of) gs in lab soon....

### Preview: PostScript

- Types: numeric, boolean, string, array, dictionary
- Operators: arithmetic, logical, graphic, ...
- Procedures
- Variables: for objects and procedures
- PostScript is just as powerful as Java, Python, ...
  - Not as intuitive
  - Easy to automatically generate
- Example: Recursive factorial procedure /fact { dup 1 gt { dup 1 sub fact mul } if } def
- Example: Drawing (see picture.ps)

Mazes

- How can we use a stack to solve a maze?
  - <u>http://www.primaryobjects.com/maze/</u>
- Properties of mazes:
  - We model a maze as a rectangular grid of cells
  - There is a start cell and one or more finish cells
  - Goal: Find path of *adjacent* free cells from *start* to *finish*
- Strategy: Consider unvisited cells as "potential tasks"
  - Use linear structure (stack) to keep track of current path being explored

## Solving Mazes

- We'll use two objects to solve our maze:
  - Position: Info about a single cell
  - Maze: Grid of Positions
- General strategy:
  - Use stack to keep track of path from start
  - If we hit a dead end, backtrack by popping location off stack
  - Mark discarded cells to make sure we don't visit the same paths twice

## **Backtracking Search**

- Try one way (favor north and east)
- If we get stuck, go back and try a different way
- We will eventually either find a solution or exhaust all possibilities
- Also called a "depth first search"

 Lots of other algorithms that we will not explore: <u>http://www.astrolog.org/labyrnth/algrithm.htm</u>

#### A "Pseudo-Code" Sketch

// Initialization

Read cell data (free/blocked/start/finish) from file data Mark all free cells as unvisited Create an empty stack S Mark start cell as visited and push it onto stack S

While (S isn't empty && top of S isn't finish cell) current ← S.peek() // current is top of stack If (current has an unvisited neighbor x) Mark x as visited ; S.push(x) // x is explored next Else S.pop() If finish is on top of S then success else no solution

#### Is Pseudo-Code Correct?

#### Tools

- Concepts: adjacent cells; path; simple path; path length; shortest path; distance between cells; reachable from cell
- Solving a maze: is *finish* reachable from *start*?
- Theorem: The pseudo-code will either visit finish or visit every free cell reachable from start
- **Proof:** Prove that if algorithm does *not* visit *finish* then it *does* visit every free cell reachable from *start* 
  - Do this by induction on distance of free cell from start
  - Base case: distance 0. Easy
  - Induction: Assume every reachable free cell of distance at most k ≥ 0 from start is visited. Prove for k+1

#### Is Pseudo-Code Correct?

- Induction Hyp: Assume every reachable free cell of distance at most k ≥ 0 from start is visited.
- Induction Step: Prove that every reachable free cell of distance k+1 from start is visited.
  - Let c be a free cell of distance k+l reachable from start
  - Then c has a free neighbor d that is distance k from start and reachable from start
  - But then by induction, *d* is visited, so it was put on stack
  - So each free neighbor of *d* is visited by algorithm
- Done!

#### Recursive "Pseudo-Code" Sketch

Boolean RecSolve(Maze m, Position current) If (current eqauls finish) return true Mark current as visited next ← some unvisited neighbor of current (or null if none left) While (next does not equal null && recSolve(m, next) is false) next ← some unvisited neighbor of current(or null if none left) Return next ≠ null

- To solve maze, call: *Boolean recSolve(*m, start)
- To prove correct: Induction on distance from *current* to *finish*
- How could we generate the actual solution?

## Implementing A Maze Solver

- Iteratively: Maze.java
- Recursively: RecMaze.java
  - Recursive method keeps an implicit stack
    - The method call stack
  - Each recursive call adds to the stack

#### Implementation: Position class

- Represent position in maze as (x,y) coordinate
- class Position has several relevant methods:
  - Find a neighbor
    - Position getNorth(), getSouth(), getEast(), getWest()
  - boolean equals()
  - Check states of position
    - boolean isVisited(), isOpen()
  - Set states of position
    - void visit(), setOpen(boolean b)

#### Maze class

#### • Relevant Maze methods:

- Maze(String filename)
  - Constructor; takes file describing maze as input
- void visit(Position p)
  - Visit position p in maze
- boolean isVisited(Position p)
  - Returns true iff p has been visited before
- Position start(), finish()
  - Return start /finish positions
- Position nextAdjacent(Position p)
  - Return next unvisited neighbor of p---or null if none
- boolean isClear(Position p)
  - Returns true iff p is a valid move and is not a wall

## Method Call Stacks

- In JVM, need to keep track of method calls
- JVM maintains stack of method invocations (called frames)
- Stack of frames
  - Receiver object, parameters, local variables
- On method call
  - Push new frame, fill in parameters, run code
- Exceptions print out stack
- Example: StackEx.java
- Recursive calls recurse too far: StackOverflowException
  - Overflow.java

#### **Recursive Call Stacks**

```
public static long factorial(int n) {
    if (n <= 1) // base case
        return 1;
    else
        return n * factorial(n - 1);
}
public static void main(String args[]) {
    System.out.println(factorial(3)};</pre>
```

}