

## Computer Science 134C

*Introduction to Computer Science, in Python*

Lecture #23 (Sorting)

November 7

<b>Keywords</b> sort, exchange, keys
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We work on developing a selection of sorts.

1. Questions?
2. Sorting techniques we consider (see Lecture 22 for details):
  - (a) Bubble sort. An attempt to reverse each out-of-order pair, in several passes.
  - (b) Selection sort. Like bubble sort, but in each pass *only the maximum value is exchanged to place it in its final position.*
  - (c) Insertion sort. A collection of sorted values is built up by inserting a new, random value in each pass. Compare with selection sort by observing the movement of maximum values.
  - (d) Quicksort. A low and high values are segregated and then considered recursively.
  - (e) Mergesort. A recursive sort that builds order from individual values upward
3. A few notes on big-O notation.
  - (a) We can frequently *bound above* some performance statistic by a mathematical function of problem size. Computer scientists are not concerned about the *exact* performance, but the dominant trend suggested by a curve.
  - (b) When a function is a sum of several components, we ignore all by that component that is dominant in the limit. For polynomials, we select the leading term. Thus, a program that takes  $n^2 + \log n$  time is described as an  $O(n^2)$  algorithm.
  - (c) Additionally, we generally don't concern ourselves with multiplicative constants. They can generally be ignored. Thus a program that makes use of  $5n$  storage locations is described as  $O(n)$  ("linear") in its space use.
  - (d) Many of our early programs ("Hello world", "counting to 10") have used constant amounts of space. We write a constant bound as  $O(1)$ .
  - (e) Programs that print out tables of simple calculations (like "counting to 10") frequently take  $O(n)$  or "linear" amounts of time.
  - (f) *Tractable* problems using one computer are typically limited to running time that is a small power of the problem size. For example, multiplying two  $n \times n$  matrices seems to take no more than  $O(n^{2.5})$  time, and requires no more than  $O(n^2)$  space.
  - (g) When we print the first  $n$  integers, their width, the number of digits, grows as  $O(\log n)$ .
  - (h) The total number of digits printed is  $O(n \log n)$ . Most fast sorts of  $n$  values take  $O(n \log n)$  time *when using one computer.*
  - (i) We can pack  $n$  equal-sized discs into a small square whose side is  $O(\sqrt{n})$ .